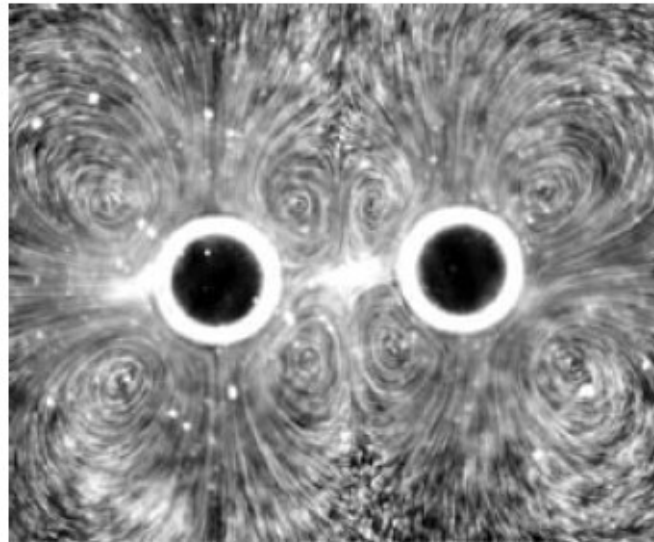


Fluid flows driven by sound and their applications

Richard Manasseh

Mechanical Engineering

Swinburne University of Technology, Melbourne, Australia



1. Mean flows driven by fluid oscillations

Co-authors

**Pauline Lai¹, Paul Tho^{1,2}, James Collis¹, Karolina Petkovic-Duran²,
Yonggang Zhu², Wah-Chin Boon³, Tim Aumann³, Malcolm Horne³, Thomas
Leong^{4,5,6}, Anthony Novell⁷, Muthupandian Ashokkumar⁵, Sandra Kentish⁶,
Ayache Bouakaz⁷, Andrew Ooi¹**

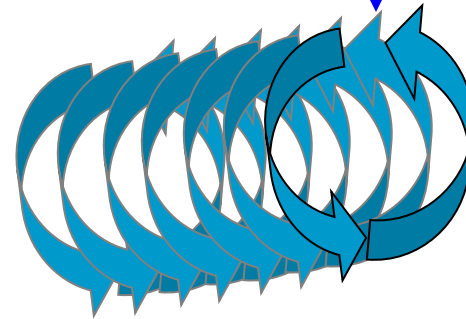
1. Mechanical Engineering, University of Melbourne, Australia
2. CSIRO Fluid Dynamics Group, Melbourne, Australia
3. Florey Neurosciences Institutes, Melbourne, Australia
4. Mechanical Engineering, Swinburne University of Technology, Melbourne, Australia
5. Chemistry, University of Melbourne, Australia
6. Chemical and Biomolecular Engineering, University of Melbourne, Australia
7. UMR Inserm U930, Université François Rabelais, Tours, France

1. Mean flows driven by fluid oscillations

Conservation of momentum in liquid (Euler)

$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial r} = - \frac{1}{\rho} \frac{\partial p}{\partial r}$$

Linear (small amplitude) oscillation



Nonlinear oscillation gives a net drift

Any fluid will *rectify* oscillation, giving *mean streaming*

2nd order mean flow velocities are always much lower in magnitude than 1st order oscillatory flow velocities

But the mean flows *keep going*, so we can see them, unlike the oscillatory flows which cancel out

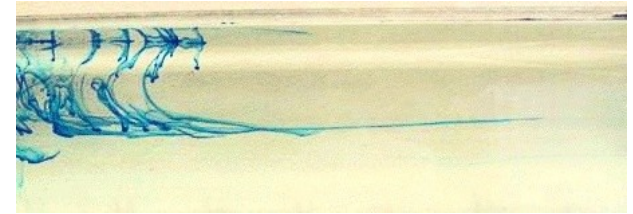
1.1. Acoustic Streaming and Microstreaming

To create a net drift, the nonlinear term must exist. Thus, a **gradient** in the acoustic field must exist.

Streaming is significant if:

- power is high (gradient provided by dissipation or spreading)

Acoustic Streaming



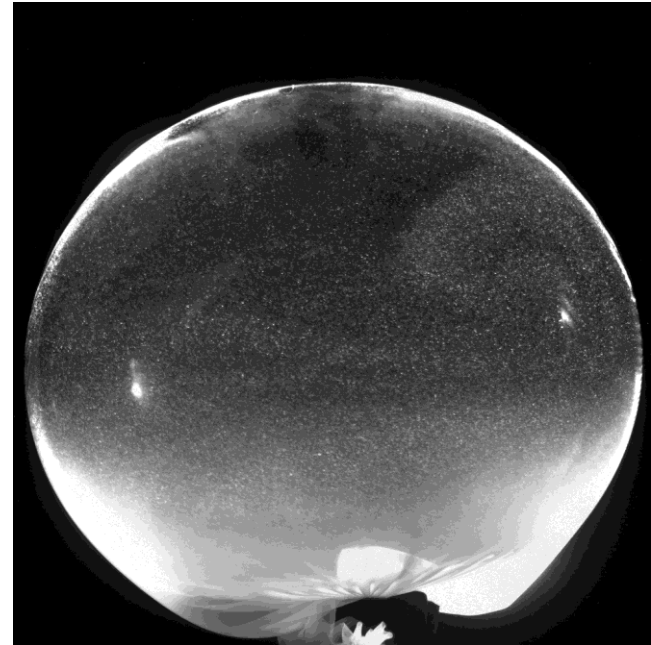
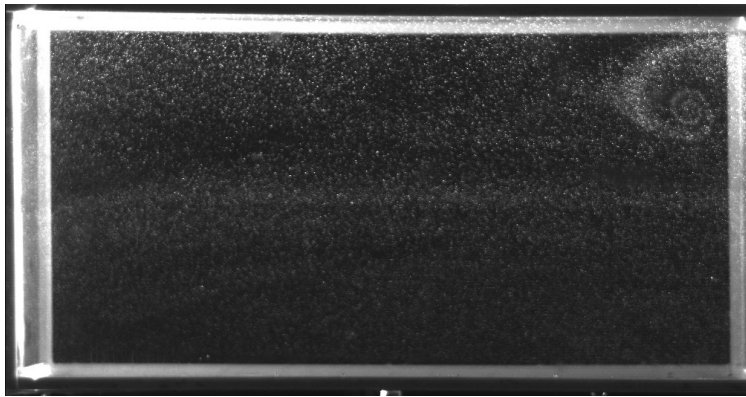
and/or

- gradient is high

Acoustic Microstreaming

2. Acoustic Streaming

Ovarian cysts

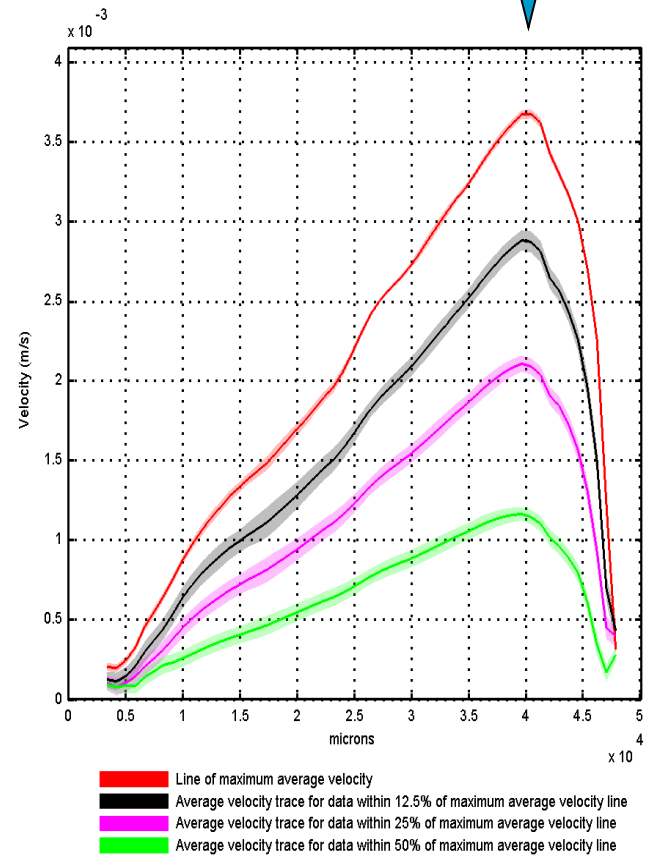
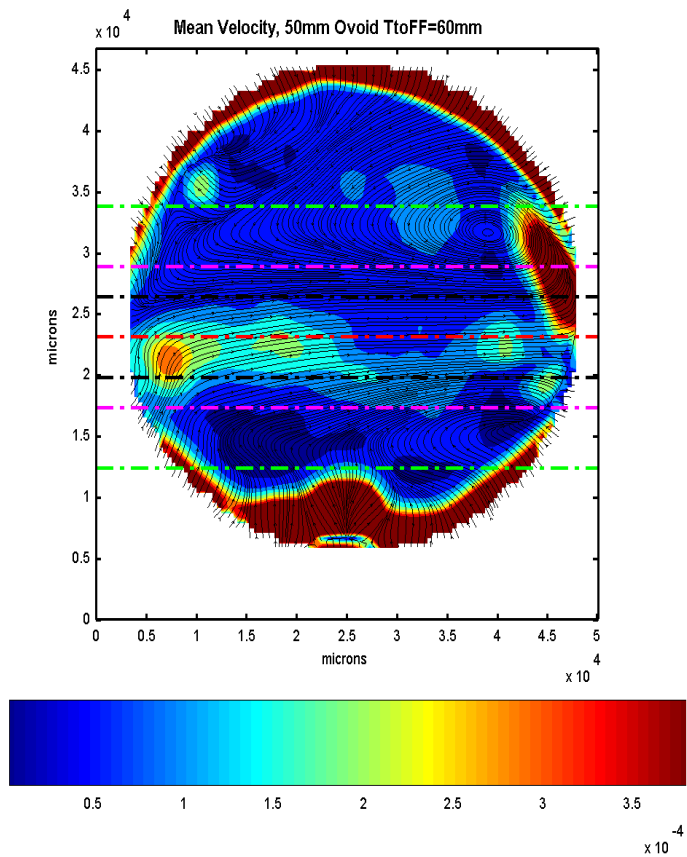


Experimental variations

- Regular geometric shapes of various types (cylinders, boxes) and ovoid shapes investigated
- Different sizes, aspect ratios and angles to the transducer beam were investigated – 31 combinations, with dimensions ranging from a few mm to 12 cm

2.1. Acoustic Streaming in medical diagnostics

Velocity profiles generally show a jet at the far wall of the cyst ... provided the cyst near face is in front of the transducer focus



1.1. Acoustic Streaming and Microstreaming

To create a net drift, the nonlinear term must exist. Thus, a **gradient** in the acoustic field must exist.

Streaming is significant if:

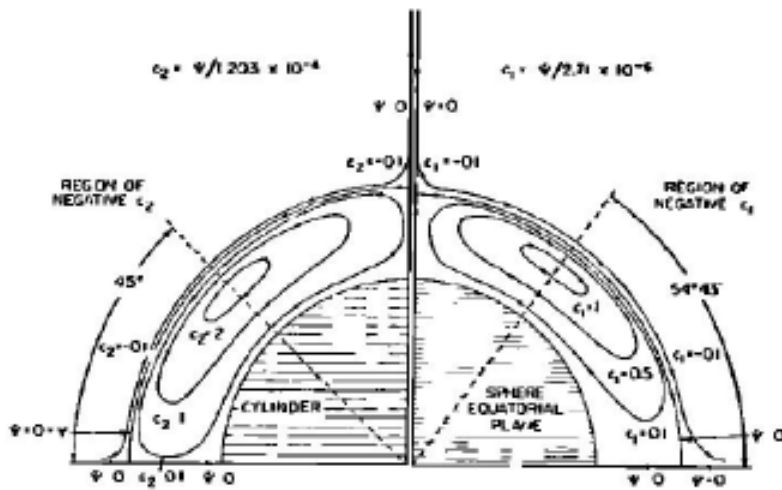
- gradient is high

**Acoustic
Microstreaming**

3.1. Acoustic microstreaming and bubbles

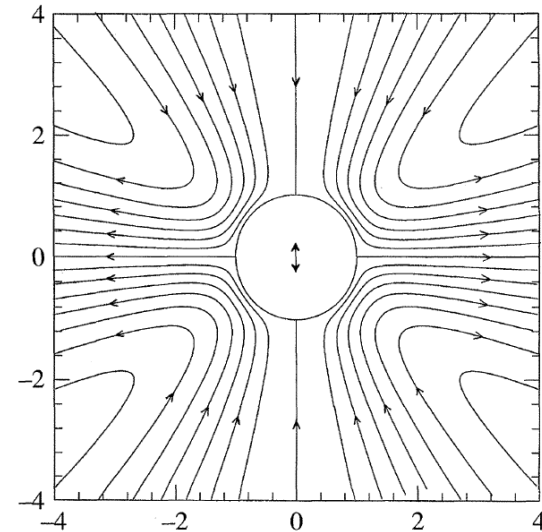
- **Primary vortices:** flow within the *Stokes boundary* or *shear wave* layer
- **Secondary vortices** flow outside boundary layer

$$\delta = \sqrt{2\nu/\Omega}$$



Primary vortices

Lane 1955, *JASA* **27**, 1082



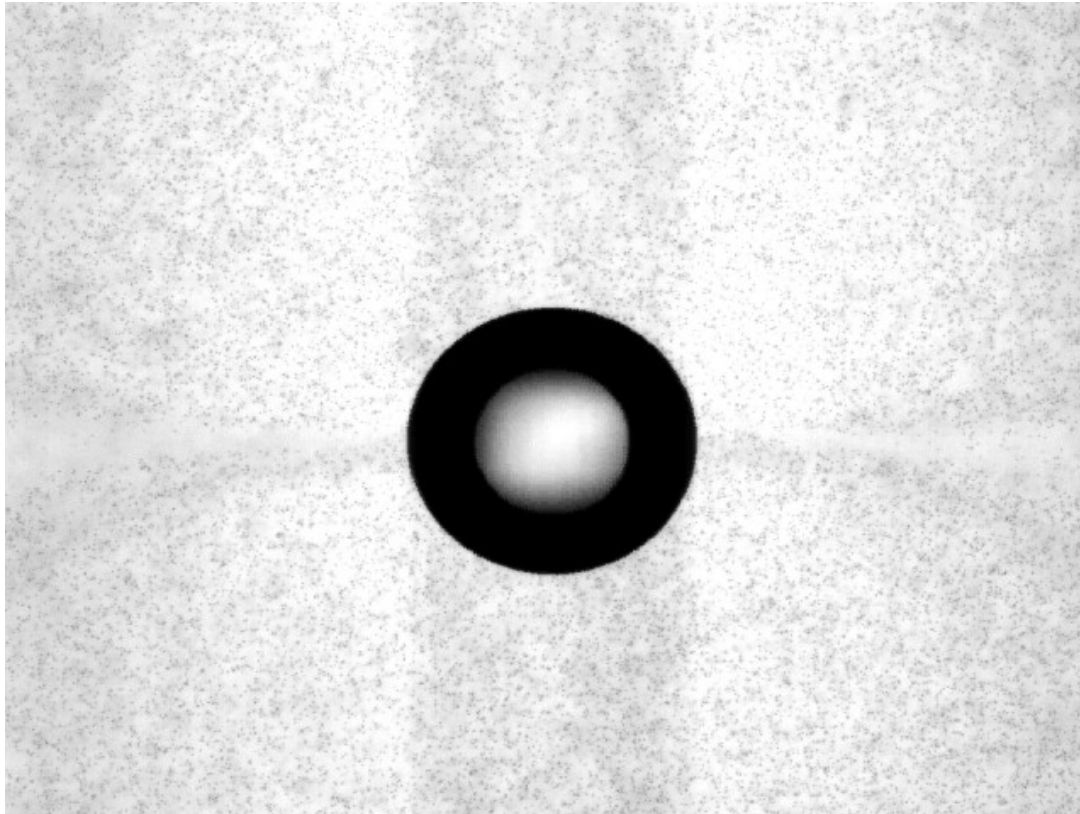
Secondary vortices

Longuet-Higgins 1998,

Proc.RSL. A, **454**, 72574

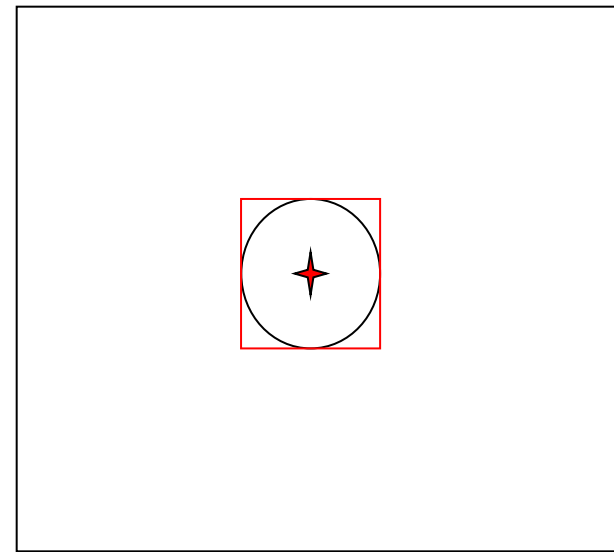
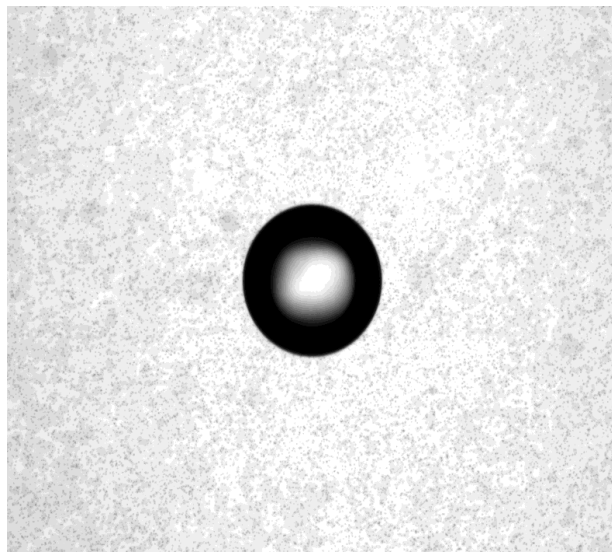
Cavitation microstreaming

- Acoustic microstreaming observed around oscillating bubbles
- The flow is observed as a system of vortices around the bubble



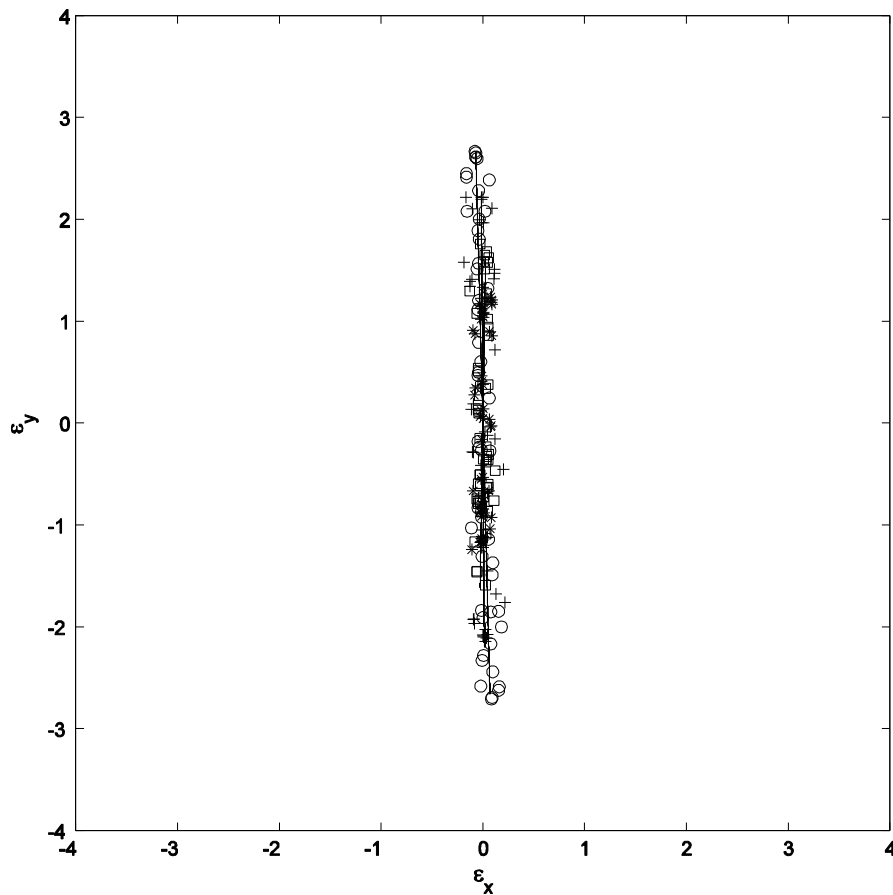
Measuring bubble motion

- Apply an edge detection algorithm to image of bubble
- Take binary image data and determine centroid of image and radius



3.1. Acoustic microstreaming and bubbles

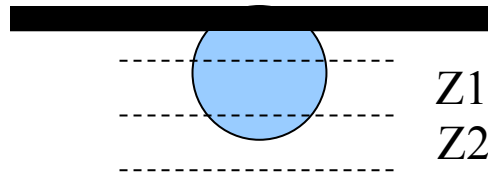
Linear translation



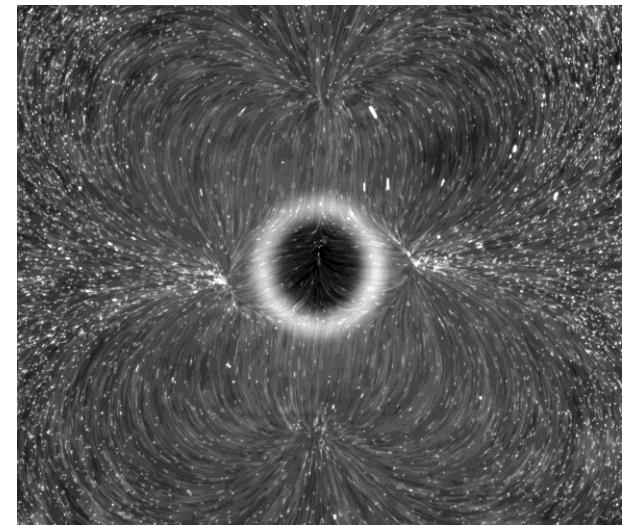
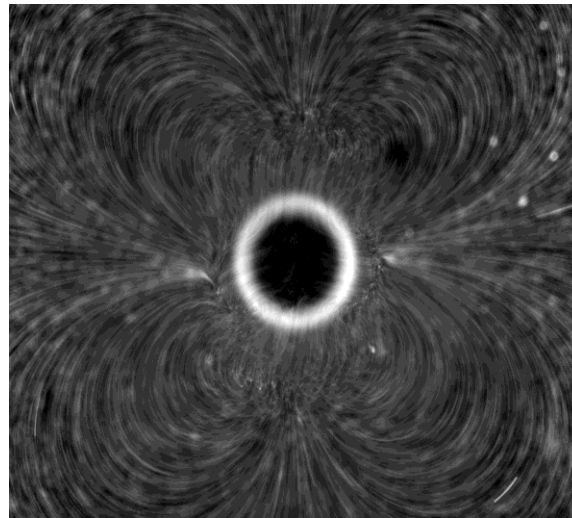
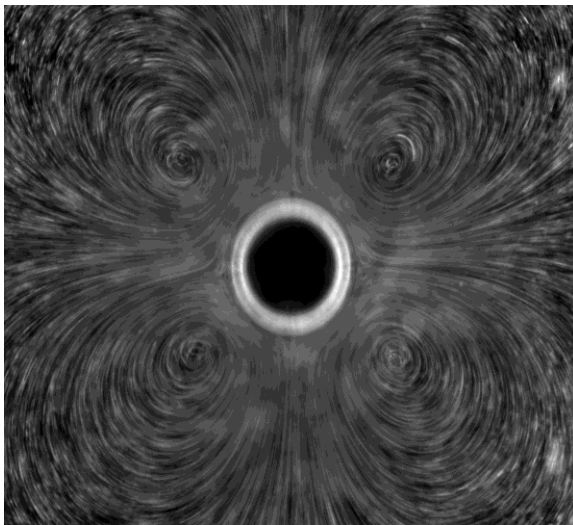
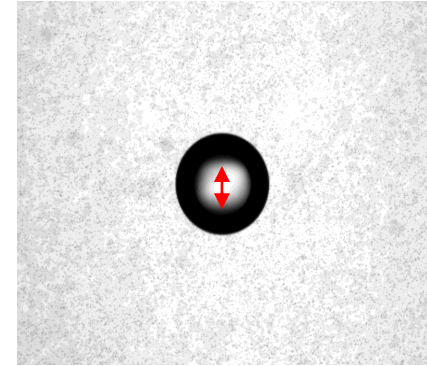
3.2. Acoustic microstreaming patterns

Linear translation

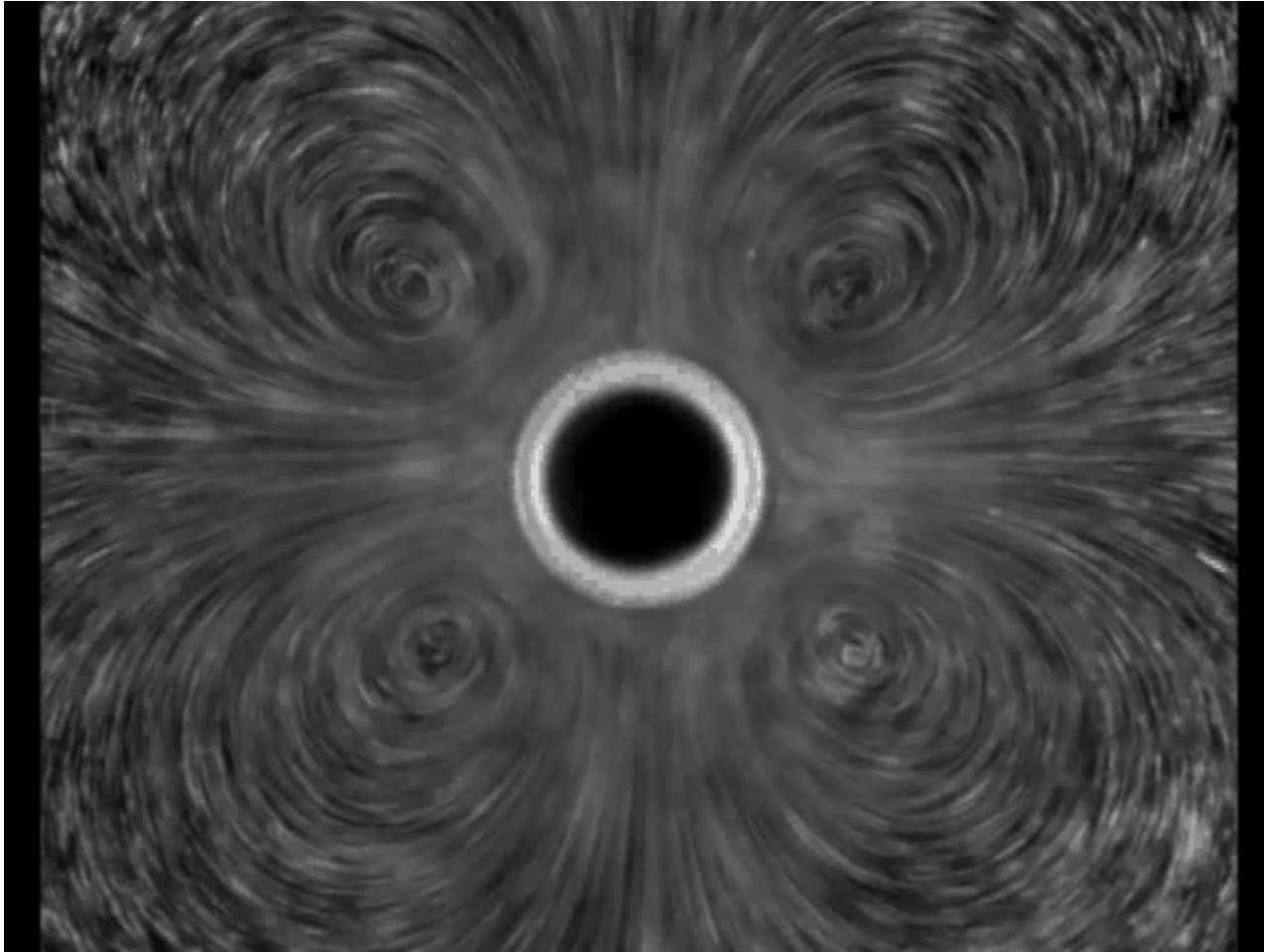
Streak photos show
3D flow



$Z_1 = 75$ microns
 $Z_2 = 250$ microns
 $Z_3 = 575$ microns



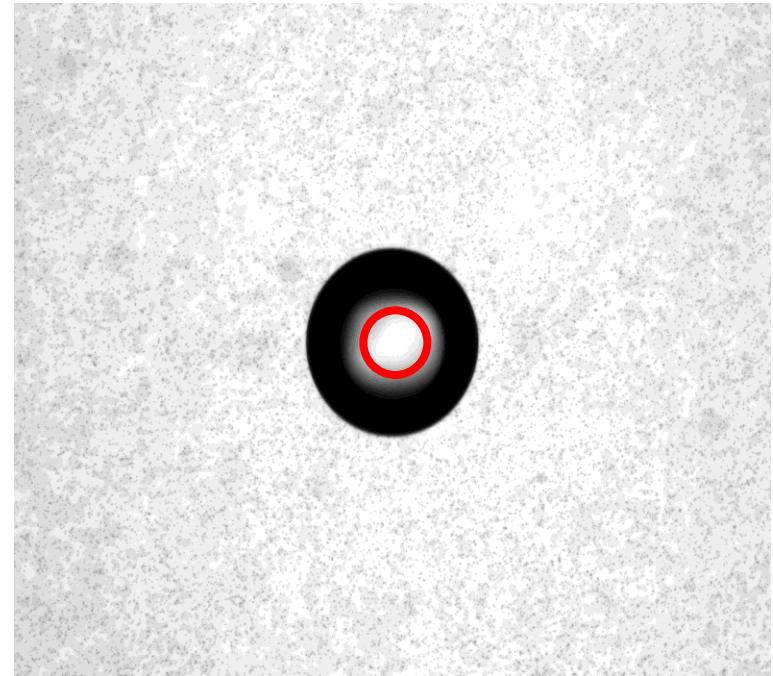
3.2. Acoustic microstreaming patterns



Tho, P., Manasseh, R., Ooi, A., 2007, *J. Fluid Mech.* 576, 191-233.

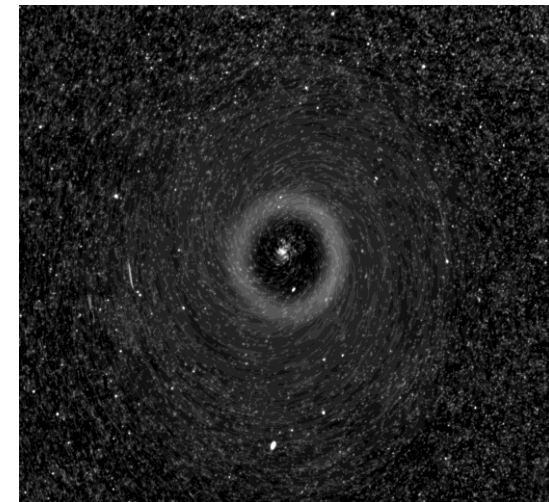
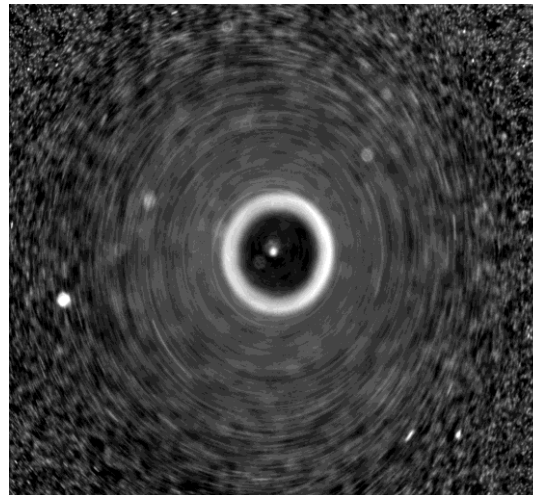
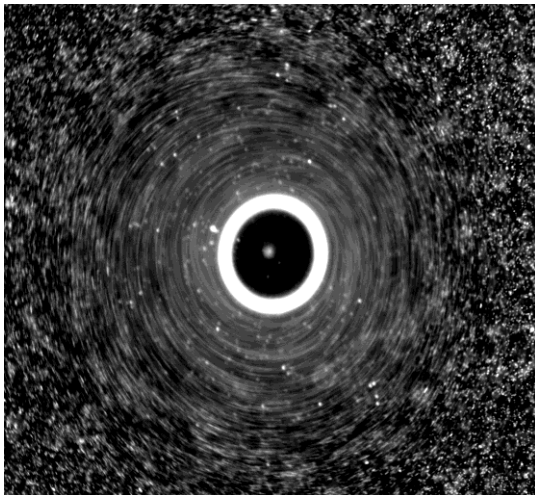
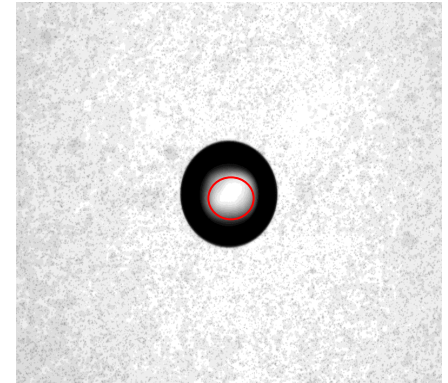
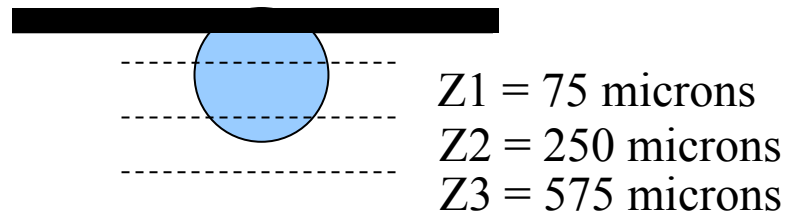
Circular orbit

- A circular orbit
- Bubble moves in anticlockwise manner

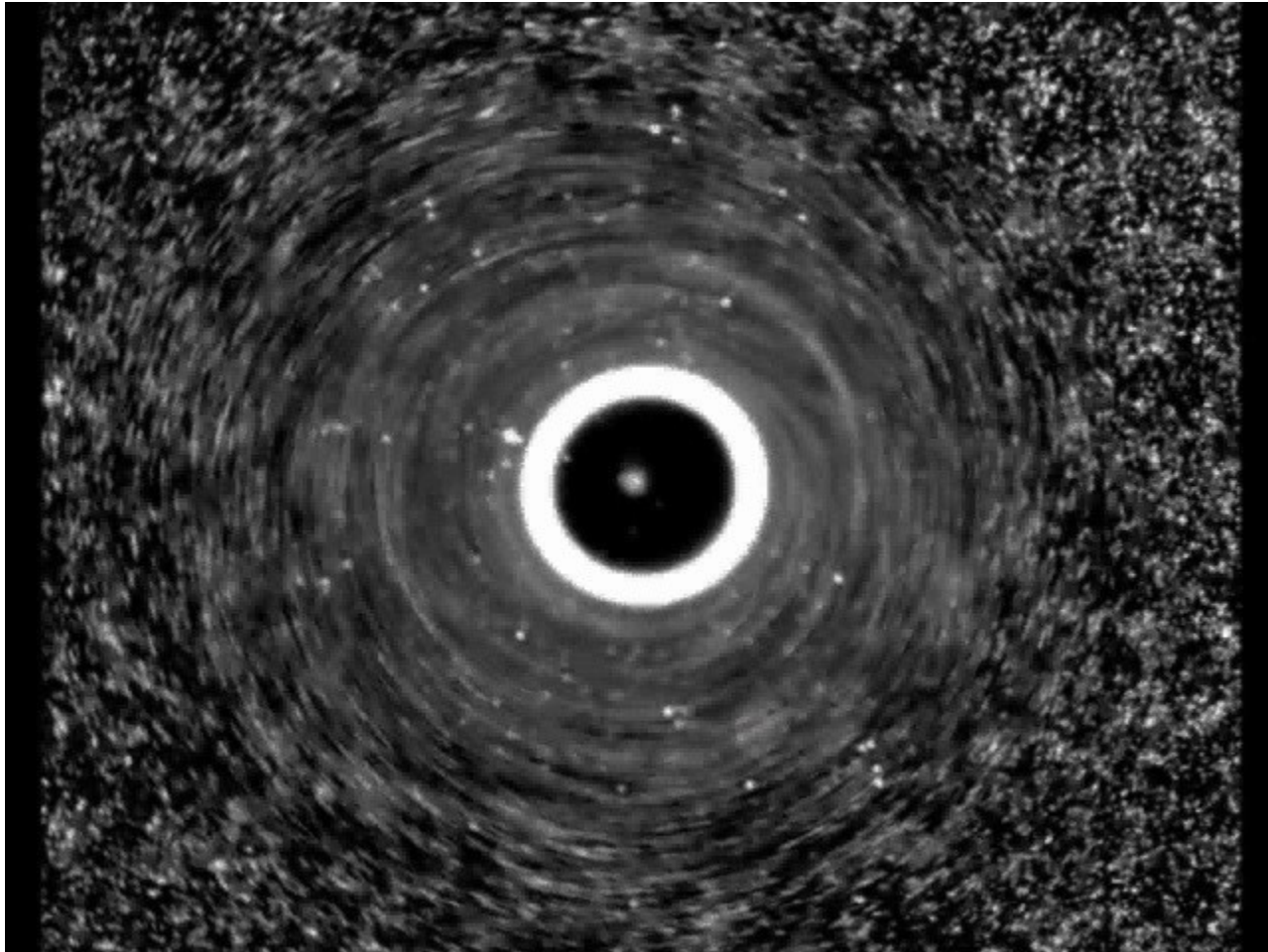


3.2. Acoustic microstreaming patterns

Circular orbit



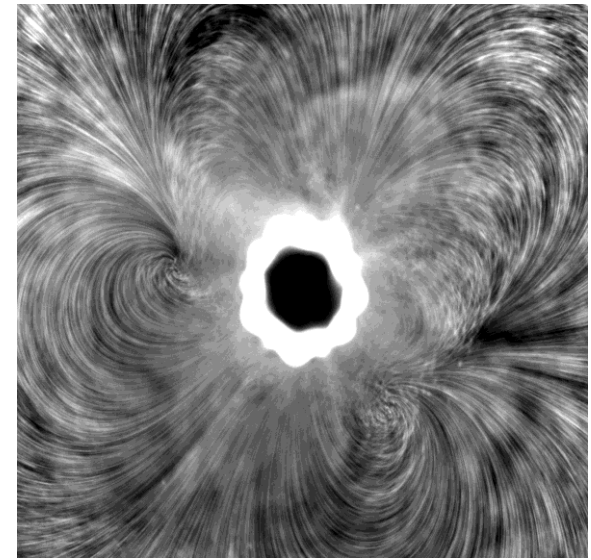
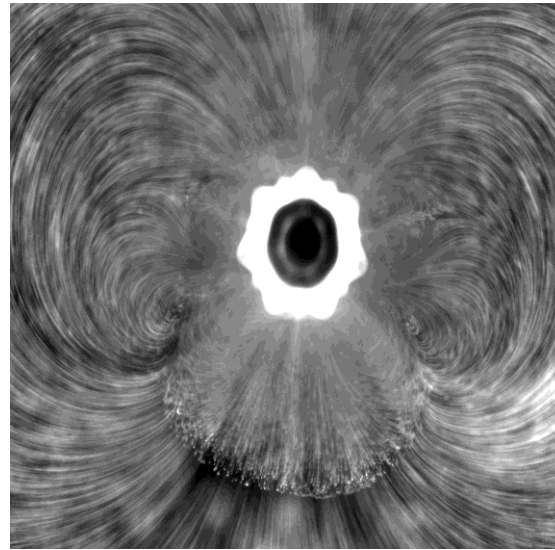
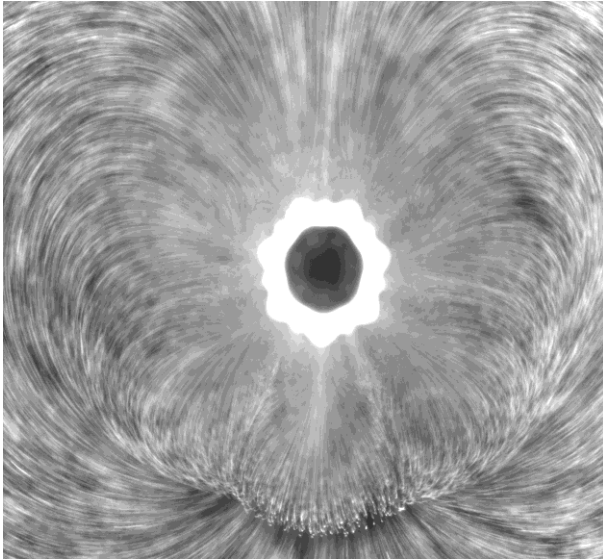
3.2. Acoustic microstreaming patterns



Tho, P., Manasseh, R., Ooi, A., 2007, *J. Fluid Mech.* 576, 191-233.

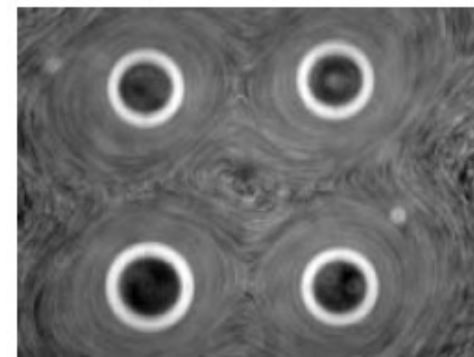
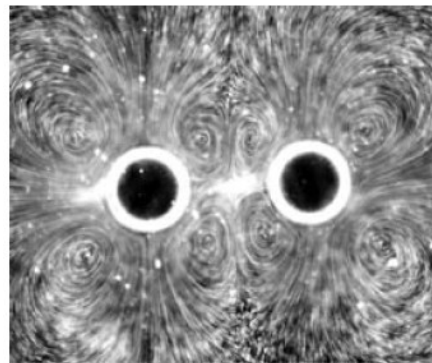
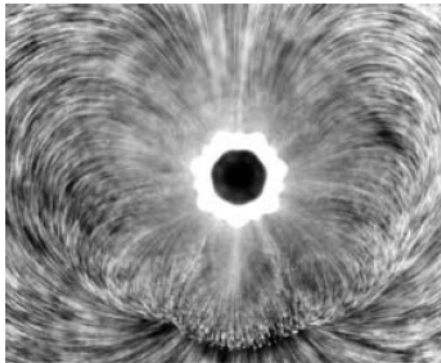
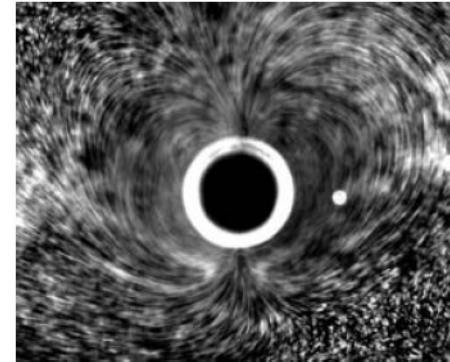
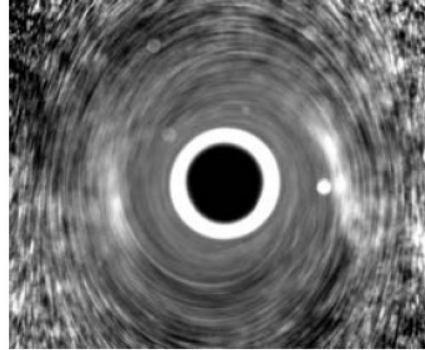
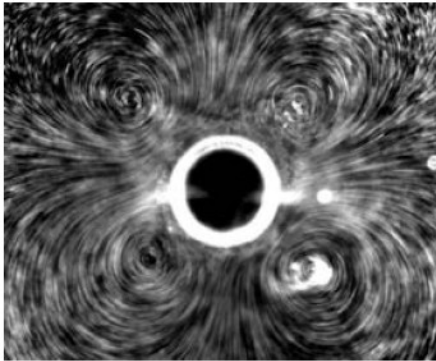
3.2. Acoustic microstreaming patterns

Shape modes



3.2. Acoustic microstreaming patterns

A variety of different flow patterns - streaklines



4. Microstreaming and micromixing

The need for chaos

- For molecules to react they must be brought into intimate contact
- Molecular diffusion is extremely slow; rate proportional to $1/L^2$.
- The regions of liquid containing reactants must be blended such that a short distance L separates them, permitting fast diffusion
- At macroscopic scales, turbulence rapidly lengthens interfaces, thinning L .

- But at microscopic scales, there is no turbulence!
- Liquids must be stirred

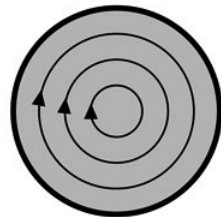
Petkovic-Duran, K., et al 2009, *Biotechniques* **47**, 827-833.

Boon, et al 2011, *Biotechniques* **50**, 116-119.

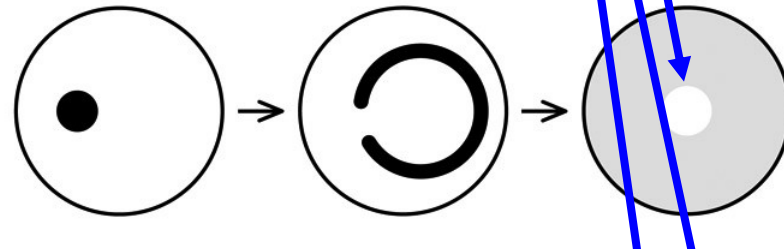
4.1. The micromixing problem

The need for chaos

Vortex



Stirring steadily with any given pattern always gives unmixed 'islands'



Petkovic-Duran, K., et al 2009, *Biotechniques* **47**, 827-833.

Boon, et al 2011, *Biotechniques* **50**, 116-119.

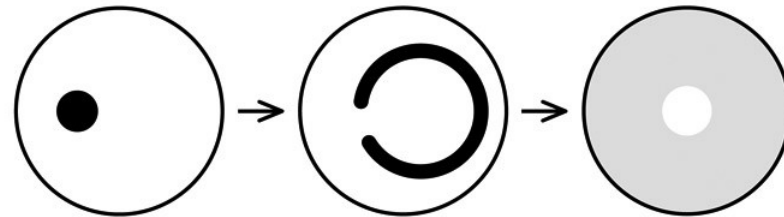
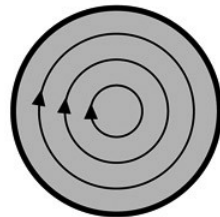
4.1. The micromixing problem

The need for chaos

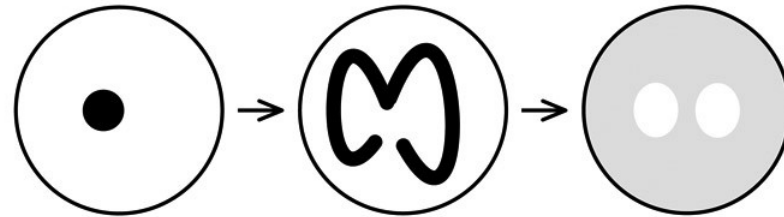
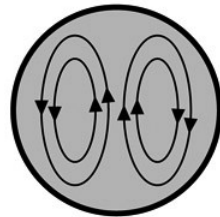
Chaotic mixing theory states that to eliminate 'islands', patterns must that have mutually intersecting streamlines must be alternated with time:

V → D → V → D → V → D → V → D →

Vortex



Dipole



Petkovic-Duran, K., et al 2009, *Biotechniques* **47**, 827-833.

Boon, et al 2011, *Biotechniques* **50**, 116-119.

4.2. Chaotic acoustic micromixing

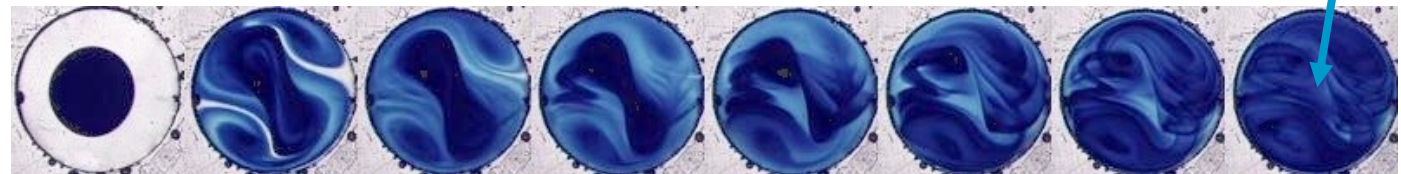
The need for chaos

Still unmixed

Vortex



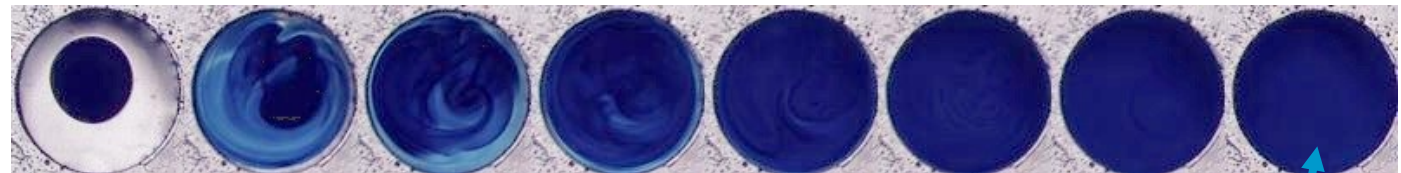
Dipole



$t=0$

3m20s

Chaotic



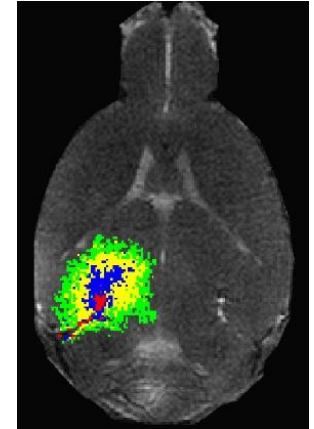
Completely mixed

Petkovic-Duran, K., et al 2009, *Biotechniques* **47**, 827-833.

Boon, et al 2011, *Biotechniques* **50**, 116-119.

5. Medical therapeutics with microbubbles

- **Sonoporation** is when molecules (DNA , drugs) that would not normally enter cells are found to enter and deliver **benefit** (gene therapy, chemotherapy) under the action of **ultrasound**
- **Sonothrombolysis** is when dangerous blood clots are dissolved or broken up under the action of **ultrasound**
- Both sonoporation and sonothrombolysis are improved when **microbubbles** are present
- **Why?**



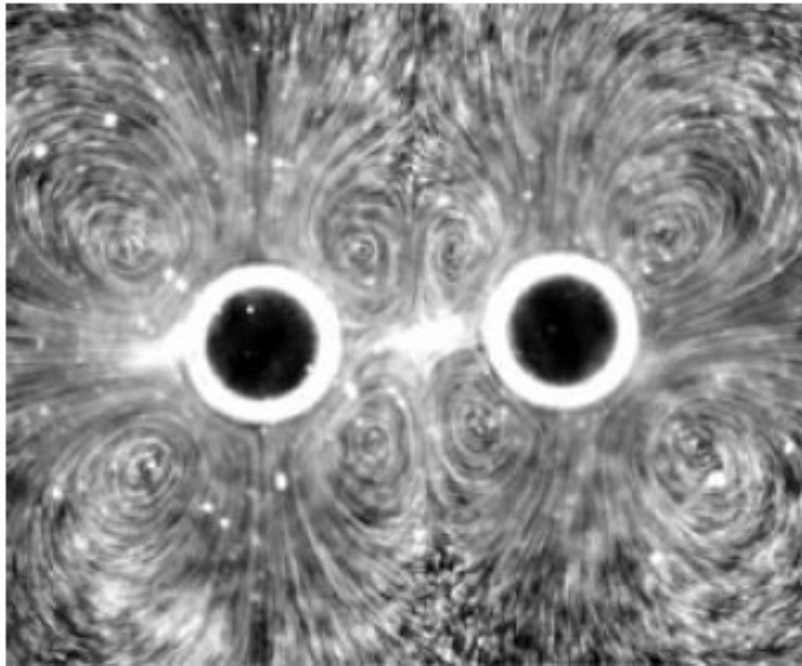
5.1. Does microstreaming help?

There are *speculations* that **microstreaming** around microbubbles creates appropriate stresses on cells, or the extracellular matrix, to cause sonoporation or sonothrombolysis

Perren et al 2008, *J. Thromb Thrombolysis*, **25**, 219-223;

Liu & Wu 2009, *JASA*. **125**, 1319-1330;

Collis et al 2010 *Ultrasonics* **50**, 273–279

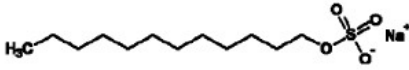
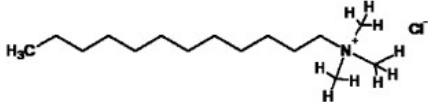
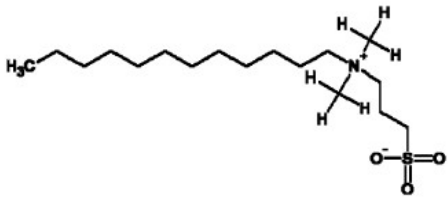


Tho et al 2007, *J. Fluid Mech.* **576**, 191-233.

- Can we understand these bioeffects?
- Can we **control** them?

5.2. Surfactants control microstreaming

- Measure microstreaming velocities quantitatively, using microPIV, in the presence of different surfactants: SDS, DTAC, DDAPS
- Surfactant concentrations adjusted to give the **same surface tension**, 50±1 mN/m, irrespective of surfactant type
- Can we affect microstreaming velocities significantly by altering surfactant type?

Surfactant	Molecular formula
Sodium dodecyl sulfate (SDS) ●	$\text{CH}_3(\text{CH}_2)_{11}\text{SO}_4\text{Na}$ 
Dodecyl dimethyl ammonium chloride (DTAC)	$\text{CH}_3(\text{CH}_2)_{11}\text{N}(\text{CH}_3)_3\text{Cl}$ 
Dodecyl dimethyl ammonium propane sulfonate (DDAPS) ▲	$\text{CH}_3(\text{CH}_2)_{11}\text{N}(\text{CH}_2)_2(\text{CH}_2)_3\text{SO}_3^-$ 

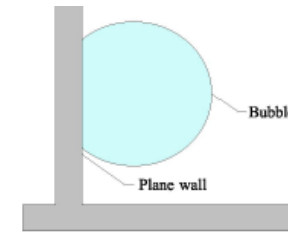
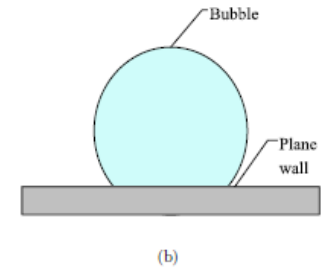
Increasing head-group size



5.2. Surfactants control microstreaming

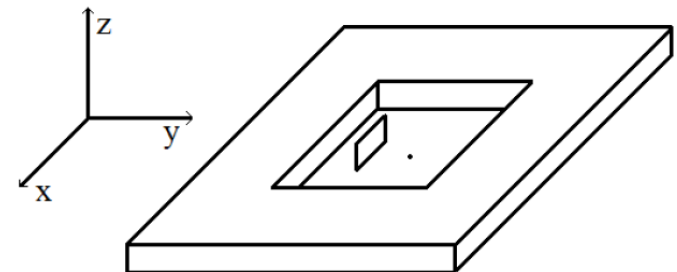
Bubbles

- Single bubbles, pendant (bottom and side)
- Formed by syringe
- 30 – 400 μm in diameter



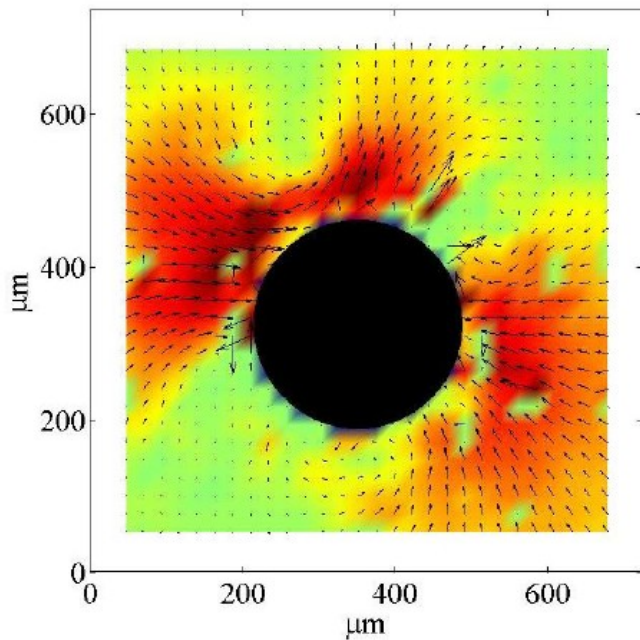
Microchamber & transducer

- 35 mm x 30 mm x (1 or 3) mm
- Additional wall to view bubble side on
- Transducer mounted onto cover
- 28 kHz CW

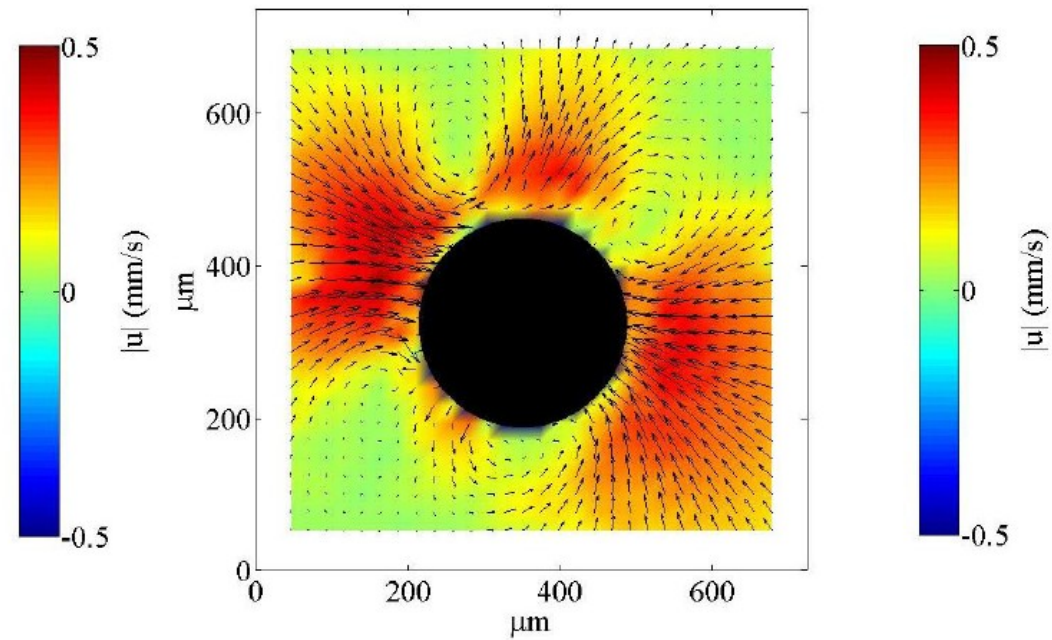


5.2. Surfactants control microstreaming

The PIV image pair were averaged over the data set to remove outliers and anomalies from the PIV analysis (30 – 200 image pairs)



1 image pair



30 image pairs

5.2. Surfactants control microstreaming

Divergence metric

The **divergence** in the ***x-y*** plane measured closest to the wall was calculated

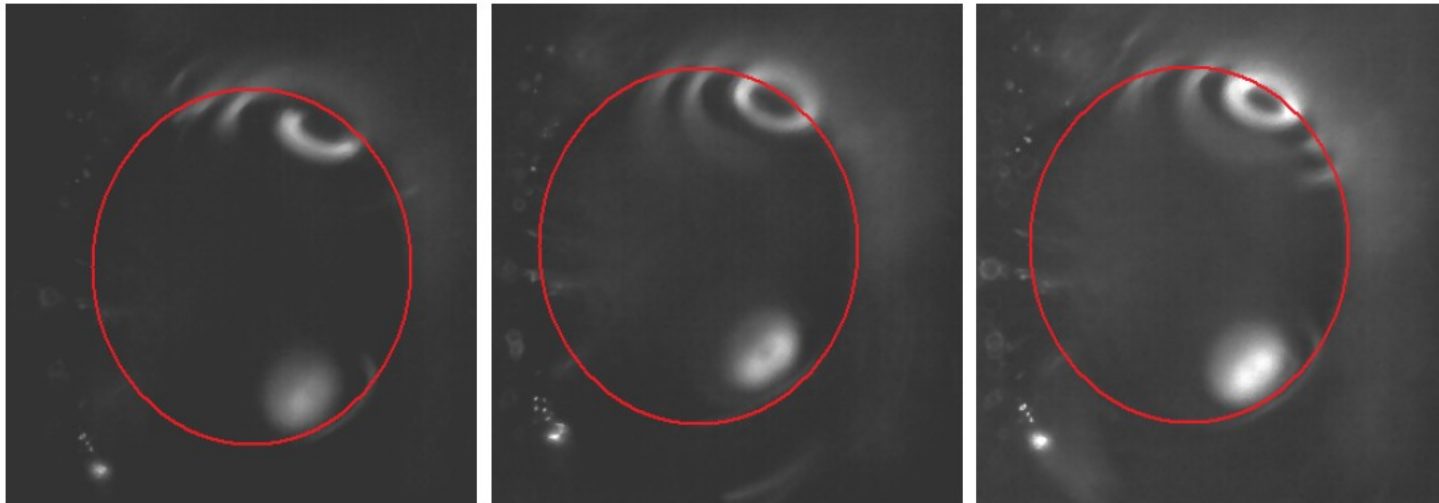
$$\nabla \cdot \mathbf{U}|_w = \left(\frac{\partial u}{\partial x}|_w + \frac{\partial v}{\partial y}|_w \right)$$

Propose that divergence represents the **stretching or compression** of a cell membrane or tissue surface that the bubble is affecting

The traditional biomedical measure is shear stress, but this is in a plane at right angles to the affected surface

5.2. Surfactants control microstreaming

- Captured on occasions PIV particles adhered to bubble surface
- Velocity = 13 ± 2 mm/s, **two orders of magnitude** greater than secondary velocity



(a)

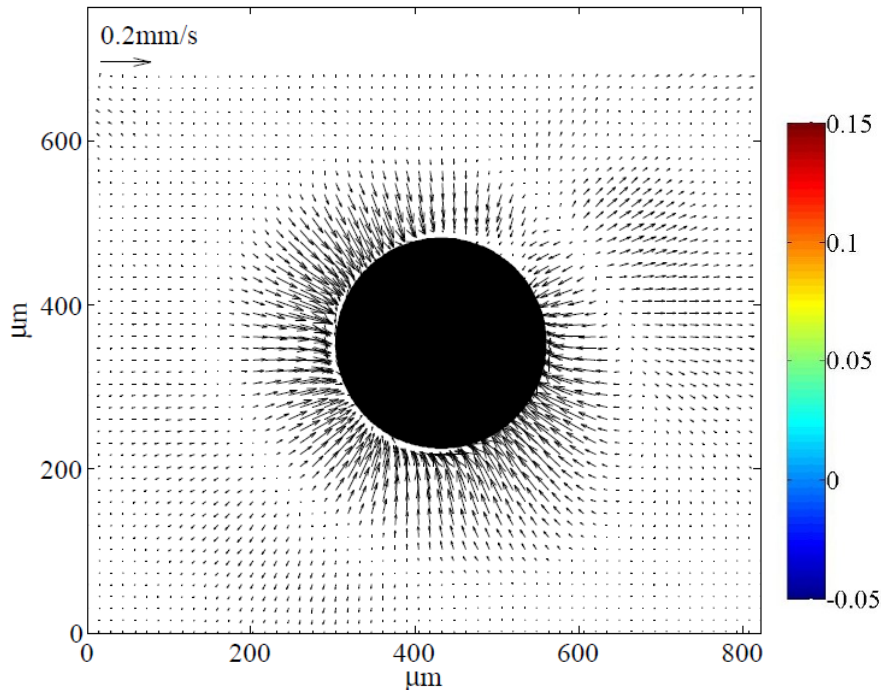
(b)

(c)

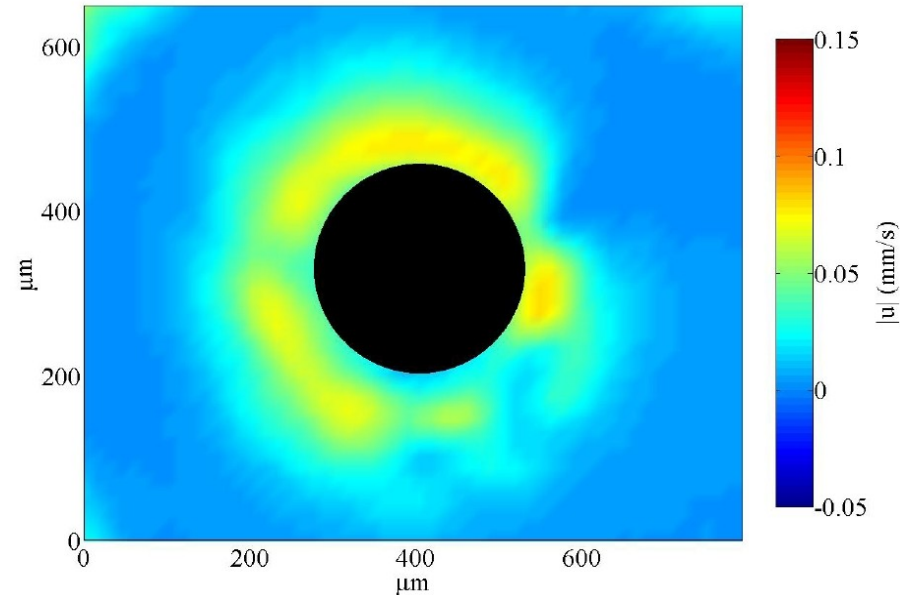
A $270 \mu\text{m}$ bubble excited at $f = 28$ kHz, amplitude = $20 V_{p-p}$ and captured in the X-Z plane with varying exposure to estimate the velocity of primary vortices at a speed of $13.35 \pm 2 \text{ mms}^{-1}$ a) exposure time of $5884 \mu\text{s}$, b) exposure time of $8322 \mu\text{s}$ c) exposure time of $11767 \mu\text{s}$

5.2. Surfactants control microstreaming

Surfactant: DDAPS



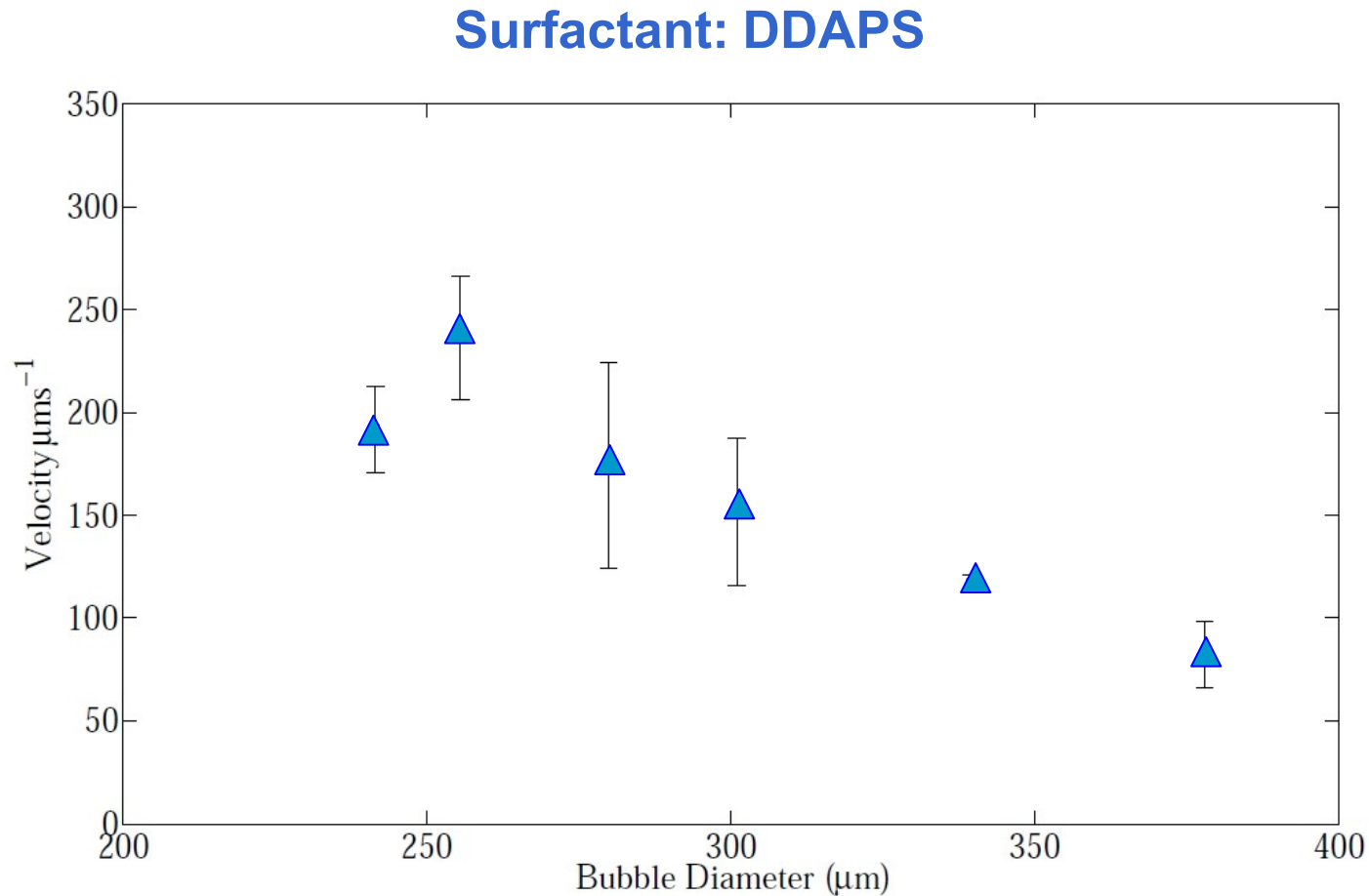
Surfactant: SDS



Velocity magnitude, bubbles driven at 28 kHz, 4.1 kPa

Recall the **surface tension is the same** (within 2%) only the **type of molecule** is different

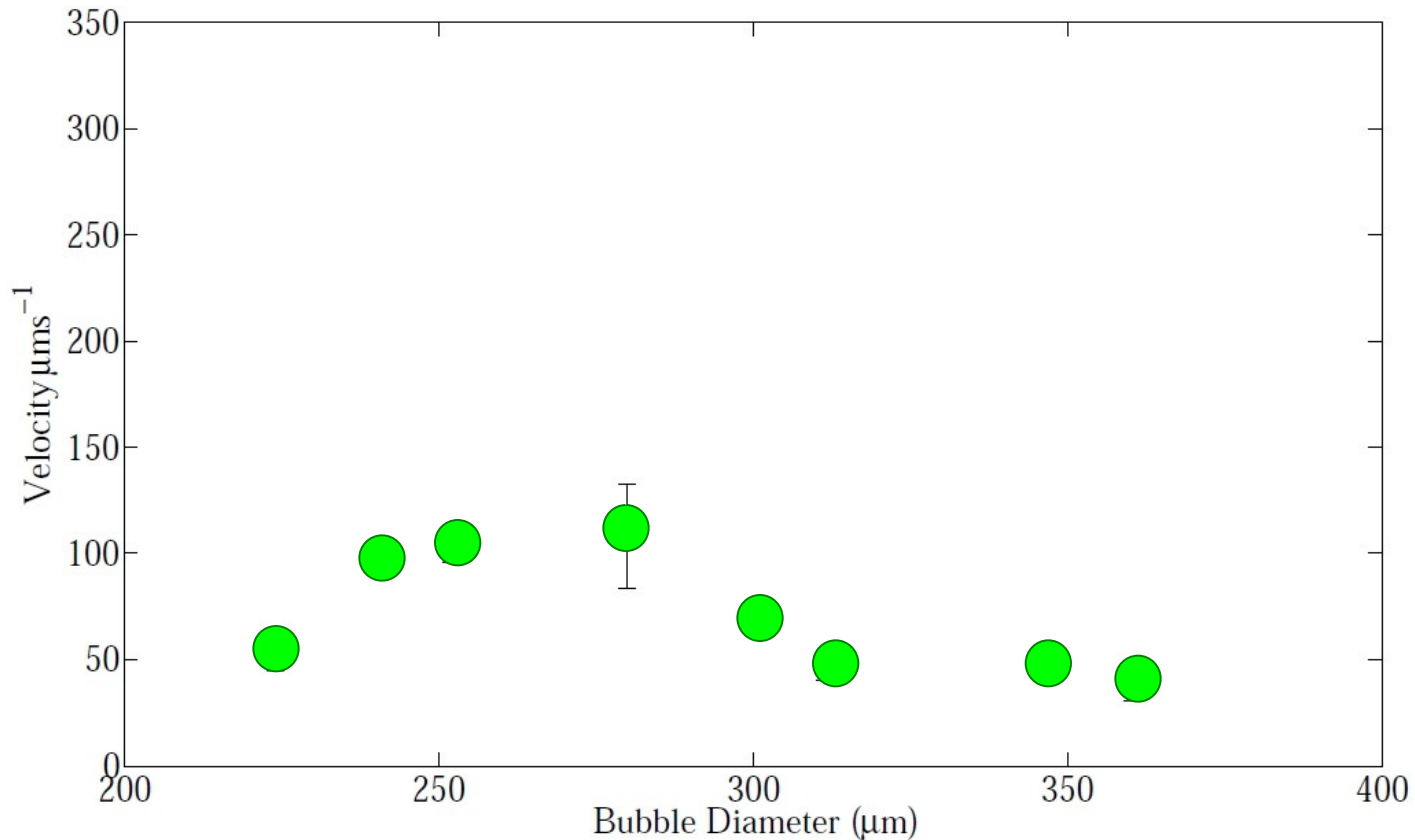
5.2. Surfactants control microstreaming



Maximum microstreaming velocities, bubbles driven at 28 kHz, 4.1 kPa

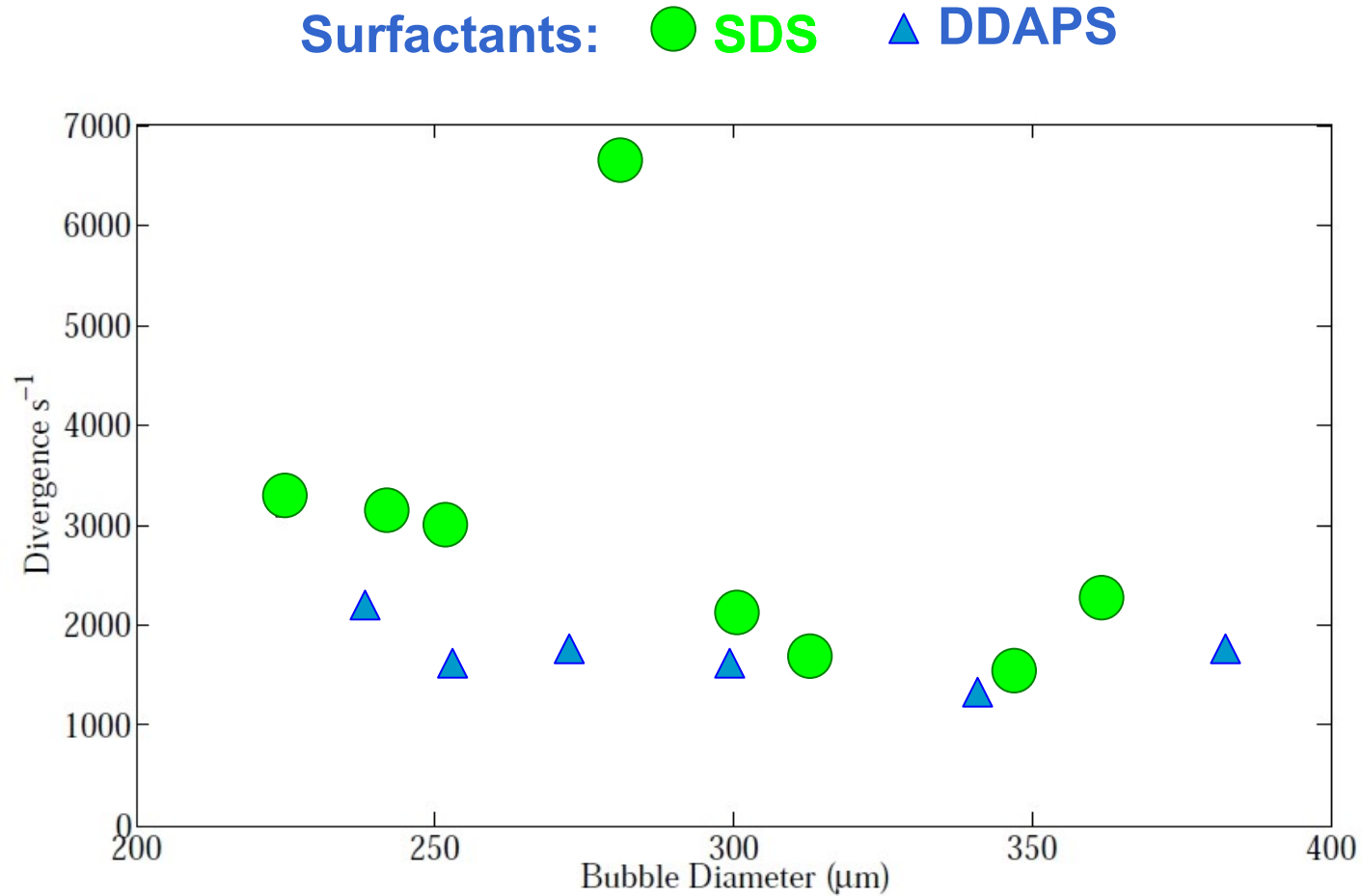
5.2. Surfactants control microstreaming

Surfactant: SDS



Maximum microstreaming velocities, bubbles driven at 28 kHz, 4.1 kPa

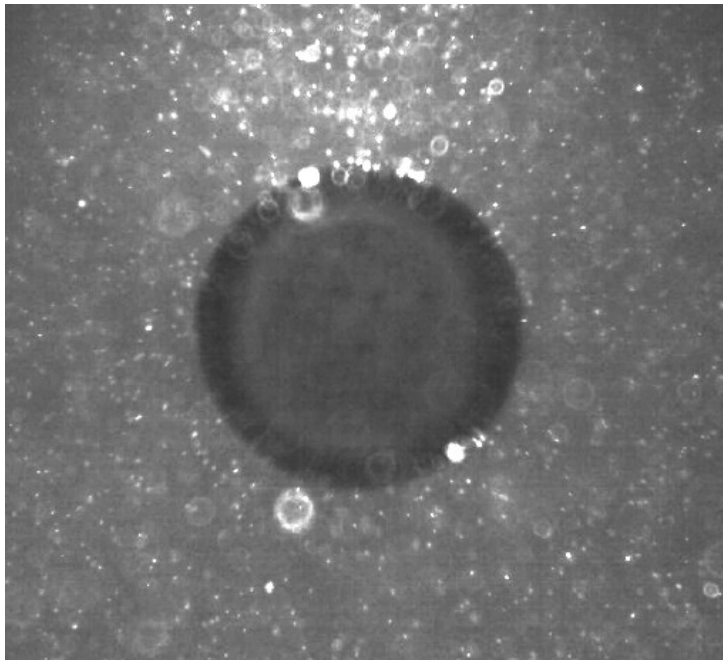
5.2. Surfactants control microstreaming



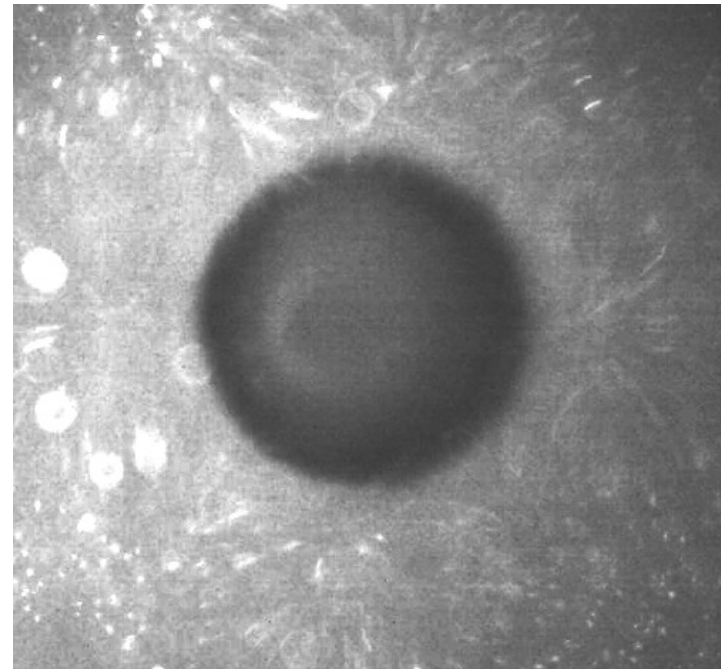
Max Divergence in the x - y plane, bubbles driven at 28 kHz, 4.1 kPa

5.2. Surfactants control microstreaming

Threshold effect under identical physical and imaging conditions



Water: low velocities



DTAC:
high velocities, surface instabilities

1. Fundamental nonlinearities create steady fluid flows when sound is applied: streaming and microstreaming
2. **Streaming** can be used for medical **diagnostics**
3. **Microstreaming** can occur in a **variety of patterns**
4. **Microstreaming** can be used for **fluid mixing** and may be relevant to new medical **therapeutics**
5. Even when the **surface tension is maintained the same**, surfactants with different molecular head groups create very **different microstreaming velocities**